

```

> restart;with(Riemann):with(Canon):with(TensorPack): CDF(0); CDS(index):
> read "EFE": read "SFE":read "fids":read "seneqs80":

```

## Chapter XX

### Using Ricci Identities

Author: Peter Huf

time propagation of SSSeq72 with p'=-1/3

SSSeq82

In this file we aim to show, assuming  $p'=-1/3$ , that the time differentiation of SSSeq72 leads to:

```
> eq[82] := -4/9 * omega^2 * theta * (Psi^2 + 1) = 0 : T(%);
```

$$-\frac{4}{9} \omega^2 \theta (\Psi^2 + 1) = 0 \quad (1.1)$$

SSSeq72 is:

```
> eq[72] : T(%);
```

$$\frac{\left(\left(\frac{3p^2}{\Psi^2} + \frac{1}{3}\right)\theta^2 - 2(\Psi^2 + 1)\omega^2 + \frac{1}{2}\mu + \frac{3}{2}p\right)p'}{\Psi^2} = \left(\frac{3p^2}{\Psi^2} + \frac{1}{3} - \frac{PUp''}{p'}\right)\omega^2 \quad (1.2)$$

```
> temp := expand(Psi^2 * subs(`p'''=0, `p''=0, `p'= -1/3, eq[72])) : T(%);
```

$$-\frac{1}{9} \frac{\theta^2}{\Psi^2} - \frac{1}{9} \theta^2 + \frac{2}{3} \Psi^2 \omega^2 + \frac{2}{3} \omega^2 - \frac{1}{6} \mu - \frac{1}{2} p = \frac{1}{3} \omega^2 + \frac{1}{3} \Psi^2 \omega^2 \quad (1.3)$$

```
> temp1 := lhs(temp) - rhs(temp) = 0 : T(%);
```

$$-\frac{1}{9} \frac{\theta^2}{\Psi^2} - \frac{1}{9} \theta^2 + \frac{1}{3} \Psi^2 \omega^2 + \frac{1}{3} \omega^2 - \frac{1}{6} \mu - \frac{1}{2} p = 0 \quad (1.4)$$

```
> temp2 := dotT(temp1) : T(%);
```

$$\begin{aligned} & -\frac{2}{9} \frac{\theta \dot{\theta}}{\Psi^2} + \frac{2}{9} \frac{\theta^2 \dot{\Psi}}{\Psi^3} - \frac{2}{9} \theta \dot{\theta} + \frac{2}{3} \Psi \dot{\Psi} \omega^2 + \frac{2}{3} \Psi^2 \omega \dot{\omega} \\ & + \frac{2}{3} \omega \dot{\omega} - \frac{1}{6} \dot{\mu} - \frac{1}{2} \dot{p} = 0 \end{aligned} \quad (1.5)$$

Now we use the following identities:

```
> temp3 := dotomega = theta * omega * `p' - 2/3 * theta * omega : T(%);
```

$$\dot{\omega} = \theta \omega p' - \frac{2}{3} \theta \omega \quad (1.6)$$

```
> temp4 := eq[65] : T(%);
```

$$\dot{\Psi} = \left( -\frac{p''\mu}{p'} - \frac{p''p}{p'} + \frac{3p^2}{\Psi^2} + \frac{1}{3} \right) \Psi \theta \quad (1.7)$$

$$> \text{temp5} := \text{subs}(\dot{\theta} = \dot{\theta}, \text{eq}[69]) : T(\%);$$

$$\dot{\theta} = \frac{3 p^2 \theta^2}{\Psi^2} \quad (1.8)$$

$$> \text{temp6} := \text{TEDS}(\mu + p = PU, \text{isolate}(\text{eq}[30], \dot{p})) : T(\%);$$

$$\dot{p} = -\theta PU \quad (1.9)$$

$$> \text{temp7} := \text{`dotp' =- `p' \cdot \theta \cdot PU : T(\%)};$$

$$\dot{p} = -p' \theta PU \quad (1.10)$$

$$>$$

$$> \text{temp8} := \text{expand}(\text{TEDS}(\text{temp7}, \text{expand}(\text{TEDS}(\text{temp6}, \text{expand}(\text{TEDS}(\text{temp5}, \text{TEDS}(\text{temp4}, \text{expand}(\text{TEDS}(\text{temp3}, \text{temp2})))))))) : T(\%);$$

$$-\frac{2}{3} \frac{\Psi^2 \mu \omega^2 p'' \theta}{p'} - \frac{2}{3} \frac{\Psi^2 \omega^2 p p'' \theta}{p'} + \frac{2}{3} \Psi^2 \omega^2 \theta p' - \frac{2}{9} \Psi^2 \omega^2 \theta + 2 p^2 \omega^2 \theta$$

$$+ \frac{2}{3} \omega^2 \theta p' - \frac{4}{9} \omega^2 \theta - \frac{2}{3} \frac{p^2 \theta^3}{\Psi^2} - \frac{2}{9} \frac{\mu p'' \theta^3}{\Psi^2 p'} - \frac{2}{9} \frac{p p'' \theta^3}{\Psi^2 p'} + \frac{1}{6} \theta PU$$

$$+ \frac{1}{2} p' \theta PU + \frac{2}{27} \frac{\theta^3}{\Psi^2} = 0$$

$$\quad (1.11)$$

$$> \text{temp9} := \text{factor}\left(\text{subs}\left(p'''=0, p''=0, p'= -\frac{1}{3}, \text{temp8}\right)\right) : T(\%);$$

$$-\frac{4}{9} \omega^2 \theta (\Psi^2 + 1) = 0 \quad (1.12)$$

$$> \text{eq}[82] := \text{temp9} : T(\%);$$

$$-\frac{4}{9} \omega^2 \theta (\Psi^2 + 1) = 0 \quad (1.13)$$

proof completed

$$>$$

$$> \text{convert}(\text{temp9}, \text{string});$$

$$"-4/9*\omega^2*\theta*(\Psi^2+1)=0" \quad (1.14)$$

>