

> restart;with(Riemann):with(TensorPack): with(Canon):CDF(0): CDS(index):

Chapter XX Tensor analysis using indices - Senovilla et al. - Shearfree for acceleration parallel to vorticity if  $\sigma_{ab}=0 \Rightarrow \omega\Theta=0$

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eq76 - time-propagation of SSSeq75

> read "EFE" : read "SFE" :read "fids" :read "Seneqs80" :

> eq[76] := theta \* (3 \* `p` + 1) \* (mu + p) = 0 : T(%);

$$\theta (3 p + 1) (\mu + p) = 0 \quad (1.1)$$

> eq[75] := (3 \* `p`^2/Psi^2 + 1/3) \* theta^2 + 1/2 \* mu + 3/2 \* p = 0 : T(%);

$$\left( \frac{3 p^2}{\Psi^2} + \frac{1}{3} \right) \theta^2 + \frac{1}{2} \mu + \frac{3}{2} p = 0 \quad (1.2)$$

>

> temp1 := expand( $\Psi^2 \cdot \text{dot}T(\text{eq}[75])$ ) : T(%);

$$6 \theta^2 p' \text{dot}p' - \frac{6 \theta^2 p^2 \text{dot}\Psi}{\Psi} + 6 \theta \text{dot}\theta p^2 + \frac{2}{3} \Psi^2 \theta \text{dot}\theta + \frac{1}{2} \Psi^2 \text{dot}\mu + \frac{3}{2} \Psi^2 \text{dot}p = 0 \quad (1.3)$$

>

we use the identities:

$$\text{dot}p = -p' \theta (\mu + p)$$

$$\text{dot}p' = -p'' \theta (\mu + p)$$

> temp2 := dotp = - `p`' . theta . (mu + p) : T(%);

$$\text{dot}p = -p' \theta (\mu + p) \quad (1.4)$$

> temp3 := `dotp`' = - `p`'' . theta . (mu + p) : T(%);

$$\text{dot}p' = -p'' \theta (\mu + p) \quad (1.5)$$

> temp4 := eq[65] : T(%);

$$\text{dot}\Psi = \left( -\frac{p'' \mu}{p'} - \frac{p'' p}{p'} + \frac{3 p^2}{\Psi^2} + \frac{1}{3} \right) \Psi \theta \quad (1.6)$$

> temp5 := TEDS(thetadot = dottheta, eq[69]) : T(%);

$$\text{dot}\theta = \frac{3 p^2 \theta^2}{\Psi^2} \quad (1.7)$$

> temp6 := dotmu = -theta . (mu + p) : T(%);

$$\text{dot}\mu = -\theta (\mu + p) \quad (1.8)$$

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>
> temp7 :=  $\frac{1}{-3 \cdot \Psi^4} \left( \text{factor} \left( 6 \cdot \Psi^2 \cdot \text{TEDS}(\text{temp6}, \text{TEDS}(\text{temp5}, \text{TEDS}(\text{temp4}, \text{TEDS}(\text{temp3}, \right. \right. \right. \right. \right. \right. \right. \left. \left. \left. \left. \left. \text{TEDS}(\text{temp2}, \text{temp1}) \right) \right) \right) \right) \right) : T(\%);$ 

$$\theta (3 p' + 1) (\mu + p) = 0$$


```

**(1.9)**

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>
>
> convert(temp7, string);
"theta*(3*'p'+1)*(mu+p) = 0"

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**(1.10)**

which is SSSeq76  
proof completed

furthermore, form SSSeq76, if  $p = -1/3$ , the SSSeq73 and 75 become

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> temp8 := expand( subs( 'p' = 1/3, 'p'' = 0, eq[73] ) ) : T(%);

$$\Psi^2 + 1 = 0$$


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**(1.11)**

which is impossible, hence  $\theta = 0$  and the theorem for this sub-case is proven.

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>

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[proof completed