

> restart;with(Riemann):with(TensorPack): with(Canon):CDF(0): CDS(index):

Chapter XX Tensor analysis using indices - Senovilla et al. - Shearfree for acceleration parallel to vorticity if $\sigma_{ab}=0 \Rightarrow \omega\Theta=0$

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eq67

> read "EFE": read "SFE": read "fids": read "Seneqs80":

proof of eq67:

$$\begin{aligned} > eq[67] := P[-a, -b] \cdot \omega[b, d, -D] = -\frac{2 \cdot p' \cdot \theta \cdot \omega[a]}{\Psi} : T(\%); \\ & P_{ab} \omega^{bd}_{;d} = -\frac{2 p' \theta \omega^a}{\Psi} \end{aligned} \quad (1.1)$$

proof: this is a simple substitution for $P[a,b]$ and eq64 into eq60

We commence with eqs61 and 64

> eq[60]: T(%);

$$P_{ab} \omega^{bd}_{;d} = -\frac{2 p' \theta \omega_a}{\Psi} - \frac{\Psi^{;d} \omega_{ad}}{\Psi} \quad (1.2)$$

> eq[64]: T(%);

$$\omega^{ab} \Psi_{;b} = 0 \quad (1.3)$$

> temp := subs(a=-a, b=-d, B=-D, eq[64]): T(%);

$$\omega_{ad} \Psi^{;d} = 0 \quad (1.4)$$

> temp2 := TEDS(temp, eq[60]): T(%);

$$P_{ab} \omega^{bd}_{;d} = -\frac{2 p' \theta \omega_a}{\Psi} \quad (1.5)$$

> temp5 := convert(temp2, string): T(%)

$$"P[-a,-b]*\omega[b,d,-D] = -2*p'*\theta*\omega[-a]/\Psi" \quad (1.6)$$

> eq[67] := parse("P[-a,-b]*\omega[b,d,-D] = -2/\Psi^2*Psi*p*'*\theta*\omega[-a]"): T(%);

$$P_{ab} \omega^{bd}_{;d} = -\frac{2 \Psi p' \theta \omega_a}{\Psi^2} \quad (1.7)$$

>

which is eq66